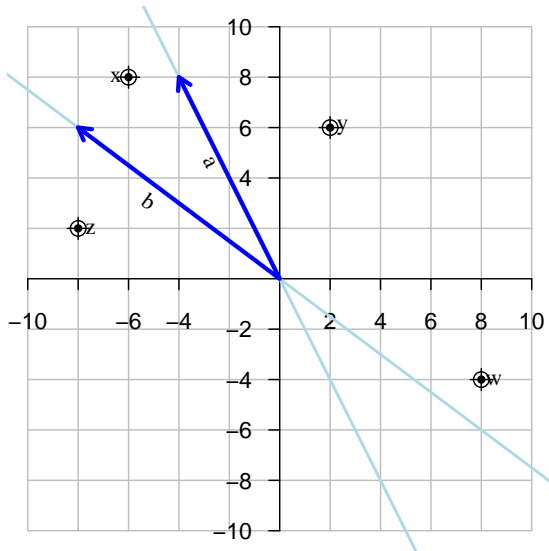


**Exer 11.1**

[V/V117]

Simpson’s paradox can be understood in terms of the geometry of the explanatory vectors and the location of the response vector, which can be thought of as a “goal” point.

The graph shows two model vectors,  $a$  and  $b$ , and several goal points. We’re going to use  $a$  and  $b$  individually, as well as both of them together. (We’ll ignore the intercept term,  $1$ , for this problem, so that we can work in two dimensions without having redundant vectors. But usually  $1$  would be included in a model.)



For each of the goal points, give the sign of the coefficient onto each of  $a$  and  $b$  individually, and then say which vector, if either, has its coefficient reversed in sign when  $a$  and  $b$  are used together to reach the goal. Simpson’s paradox occurs whenever the sign of a coefficient is reversed when another vector is added into the model.

Model Structure	Sign of Coefficient					
	on $a$			on $b$		
$x \sim a$	pos	neg	zero	- NA -		
$x \sim b$	- NA -			pos	neg	zero
$x \sim a+b$	pos	neg	zero	pos	neg	zero

TRUE or FALSE Exer 11.1-5 Is there Simpson’s paradox involved in modeling  $x$  by  $a$  and  $b$ ?

Model Structure	Sign of Coefficient	
	on $a$	on $b$
$y \sim a$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-6</small>	- NA -
$y \sim b$	- NA -	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-7</small>
$y \sim a+b$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-8</small>	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-9</small>

TRUE or FALSE Exer 11.1-10 Is there Simpson's paradox involved in modeling  $y$  by  $a$  and  $b$ ?

Model Structure	Sign of Coefficient	
	on $a$	on $b$
$w \sim a$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-11</small>	- NA -
$w \sim b$	- NA -	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-12</small>
$w \sim a+b$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-13</small>	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-14</small>

TRUE or FALSE Exer 11.1-15 Simpson's paradox is involved in modeling  $w$  by  $a$  and  $b$ .

Model Structure	Sign of Coefficient	
	on $a$	on $b$
$z \sim a$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-16</small>	- NA -
$z \sim b$	- NA -	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-17</small>
$z \sim a+b$	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-18</small>	<u>pos</u> <u>neg</u> <u>zero</u> <small>Exer 11.1-19</small>

TRUE or FALSE Exer 11.1-20 Simpson's paradox involved in modeling  $z$  by  $a$  and  $b$ .