

## Chapter 5: The Basics of Kinetic-Molecular Theory

**Goal:** Understand (on a microscopic level) the variables in  $PV=nRT$  (especially temperature)

**Assumptions** (how a physicist would describe an ideal gas...):

- (1) A gas consists of particles (that is, atoms or molecules) of negligible size.
- (2) These particles move at a variety of speeds in all directions: this gives rise to the volume a gas is said to occupy.
- (3) These particles exert no forces on each other, except during collisions.
- (4) Particles exert pressure by colliding with the walls of its container.

Then sit back as brilliant 19th century physicists (like James Clerk Maxwell and Ludwig Boltzmann) do lots of math....

**Result: Temperature determines the average kinetic energy ( $KE$ ) of a gas**

$$KE = \frac{3}{2}nRT$$

From physics, we know that

$$KE = \frac{1}{2}mu^2 = \frac{1}{2}nMu^2$$

where  $u$  is the average speed of the gas, and  $M$  is the molar mass. So

$$\frac{1}{2}nMu^2 = \frac{3}{2}nRT$$

$$Mu^2 = 3RT$$

$$u \approx \sqrt{\frac{3RT}{M}}$$