Experiment 4: Analysis of an Acid-Base Titration Curve-The Gran Plot
(Adapted from Daniel C. Harris’ Quantitative Chemical Analysis.)

Two Hours Experimental Work on Your Own (between March 31 and April 12)
(No Pre-Lab Flowchart Required—but see note below)
Notebook Due on April 18 by 5 p.m. (20% per day penalty if late)

Introduction

In this experiment, you will titrate a sample of pure potassium hydrogen phthalate (KHP, Harris Table 12-5) with NaOH. The net ionic equation for the titration is shown below:

\[
\text{hydrogen phthalate (HP\textsuperscript{-})} + \text{OH}\textsuperscript{-} \rightarrow \text{phthalate (P\textsuperscript{2-})} + \text{H}_2\text{O}
\]

The first goal of the experiment is to standardize the NaOH solution. In General Chemistry, you relied solely on the titration endpoint to determine the NaOH concentration. However, in this course, we will make use of an entire section of the titration curve to determine the endpoint with (potentially) greater accuracy. This analysis involves the construction of a Gran plot (discussed in Harris Section 12-5). The Gran plot will also let us determine an accurate value of \( K_a \) for hydrogen phthalate. (Note that this is \( K_2 \) for the fully protonated form, phthalic acid, which is listed in Harris Appendix G.) Activity coefficients (which we covered in Chapter 8) are used in the calculations for this experiment.

Experimental Procedure

Before you come to lab, the teaching assistant will have dried vials of potassium hydrogen phthalate at 105°C, and prepared an aqueous sodium hydroxide solution, which, when prepared, was 0.1000 M. You will perform the titration using the Chemistry Department’s Mettler DL12 Titrator.

Although no pre-lab flowchart is required, you are still expected to document your lab work carefully in your notebook. This includes brief descriptions of what you did, specific observations, and good notebook mechanics (page numbers and dates).

1. Take a vial of potassium hydrogen phthalate from the oven and cool the uncapped vial in a desiccator for at least 10 min.

Note the various components of the titrator as shown on the next page:
2. Meanwhile, remove the titrator pH electrode from its storage sleeve, rinse the electrode with distilled water, and carefully insert the electrode through the open hole in the titration head.

3. Calibrate the electrode as follows:
   a. Press 3 (on the numeric keypad) and ELEC CALIB (this button is in the second column from the left) on the control panel. A light bar should start blinking to the left of BUFFER A on the display panel.
   b. Attach the plastic sample cup containing red pH 4 buffer by loosening the grey retaining ring on the titration head (by turning the ring clockwise), raising the cup until it catches, and gently tightening the ring (by turning it counterclockwise) while holding the cup in place.
   c. Press the green START button at the lower right of the control panel. If everything goes well, after a few seconds, a light bar should start blinking to the left of BUFFER B on the display panel.
   d. Holding the plastic sample cup in place, loosen the grey retaining ring and remove the sample cup. Rinse the electrode, buret tip, and stirrer thoroughly with distilled water (holding a waste beaker under the titration head), then mount the sample cup containing purple pH 10 buffer.
   e. Again, press the green START button at the lower right of the control panel. If everything goes well, after a few seconds, you should hear three beeps, confirming that the calibration was a success!
   f. Remove the sample cup containing the pH 10 buffer, and rinse the electrode, buret tip, and
stirrer as before.

4. Using an analytical balance, weigh out close to 0.3000 g of the potassium hydrogen phthalate (KHP), and transfer into a 50-mL volumetric flask. Add some distilled water to the flask and completely dissolve the solute. Then dilute to the mark with more distilled water.

5. Pour the 50 mL of KHP solution into a clean, dry sample cup. **Be sure to add two drops of phenolphthalein indicator to this solution!**

6. Mount the sample cup onto the titration head, then press the **STIR** button (in the second column from the left on the control panel).

7. Now take a few moments to calculate a theoretical equivalence point based on the reported $[\text{OH}^-]$ and the mass of KHP (FW 204.22). (Obviously, you should do this in your notebook and not on some random scrap of paper!)

8. Press the **MAIN TITR** button on the rightmost column of the control panel. The display panel will show the pH of the solution to three decimal places. Record the pH after ~15 seconds. (This is the pH value with 0 mL of titrant added.)

9. Press the **mL pH** button (in the third column from the left on the control panel) to toggle the display readout to mL. Press and hold down the **MAIN TITR** button until the display reads 1.50 mL. The electronic buret will add precisely that amount of NaOH to the sample cup. Write down that volume. Press the **mL pH** button, wait 15 seconds, and write down the pH.

10. Press the **mL pH** button. Then press and hold down the **MAIN TITR** button until the display reads 3.00 mL. Write down that volume. Press the **mL pH** button, wait 15 seconds, and write down the pH.

11. Until you are within ~3 mL of the equivalence point, continue adding base in 1.50-mL aliquots, recording the volume (to the nearest 0.01 mL) and the pH (to three decimal places) 15 s after each addition.

12. Thereafter, use 0.40-mL increments until you are within 1 mL of the equivalence point. After each delivery of titrant, record the titrant volume and the pH (waiting 15 s each time).

13. At 1 mL before the equivalence point, you should start adding base only 0.01 mL at a time. However, you only need to record the pH every 0.10 mL. The reason you are adding base so slowly is that you want to determine (and write down) the volume at which the very first faint pink color is observed. Once the phenolphthalein end point is reached, add three more 0.10-mL aliquots, recording the pH each time (after waiting 15 s). (Question: Why is it not surprising that the pH readings are becoming increasingly unstable in this part of the titration curve?)

14. Finally, add three more 1.00-mL aliquots. After each delivery of titrant, record the titrant volume and the pH (yes, you should still wait 15 s before recording each pH reading).

15. When you have collected all your data, press **RESET**. Remove the sample cup, rinse it several times with distilled water, and dry. (Do not use any soap!) Leave the cup next to the titrator.

16. Rinse the buret tip, stirrer, and electrode thoroughly. Carefully remove the electrode from the titration head and return the electrode to its storage sleeve.

17. Clean up the rest of your glassware (leftover KHP can go down the sink). Leave the titrator turned on.
**Data Analysis**

Note: Except for the $K_a$ value, do not worry about calculating uncertainties for your results.

(1) Plot all of the data from your titration, and paste a copy of your plot into your notebook:

**Titration of Potassium Hydrogen Phthalate by ~0.1 M NaOH**

(2) Report your titration endpoints as determined by (a) the indicator and (b) a first derivative plot (see pp. 237-238 of your text). Your notebook should include a plot like this:

**First Derivative of Titration Curve**
(3) As we discussed in class, NaOH is not a primary standard. Although the KHP was the “analyte” in your titration, it is actually used to standardize (that is, determine the concentration of) the NaOH solution. Use your phenolphthalein and first derivative endpoints to calculate two estimates of the concentration of the NaOH solution (to four significant figures). Discuss qualitatively the differences among the formal (i.e. 0.1000 M), phenolphthalein-based, and first-derivative-based concentrations.

(4) Construct a Gran plot \(V_{\text{titrant}} 10^{-pH} \text{ vs. } V_{\text{titrant}}\). Plot for \(V_{\text{titrant}}\) ranging from ~0.8\(V_e\) to past \(V_e\). You should use either your phenolphthalein or first derivative endpoint (whichever you have more confidence in) as your \(V_e\) value. Include a copy of the following plot in your notebook:

![Preliminary Gran Plot for Titration--0.8 Ve to past Ve](image)

(The plot becomes non-linear when \(V_{\text{titrant}}\) is very close to \(V_e\). This is largely due to the breakdown of our assumption that mol P\(^2-\) = mol OH\(^-\) added. This assumption starts to fail because [HP\(^-\)] is quite low close to the endpoint. Hence, the reverse of the titration reaction, P\(^2-\) + H\(_2\)O \(\rightarrow\) HP\(^-\) + OH\(^-\), becomes non-negligible, as predicted by Le Chatelier’s Principle.)

(5) Next, we want to fit a line to only the linear part of the Gran plot. First, choose and plot a subset of the data before \(V_e\). Then add a trendline to these data. Do this (using Excel on the PC; Mac Excel may be slightly different) by...

- Selecting “Add Trendline” under the Chart pull-down menu.
- Under the “Type” tab, choose a linear Trend/Regression Type.
- Under the “Options” tab, choose to display both the equation and R-squared value on the chart. Also choose to forecast forward by 1 unit. (The idea here is, you want your trendline to cross the x-axis. The x-intercept will give you the Gran plot estimate of \(V_e\).)
- Click on your trendline box and go to Format Selected Data Labels. Under the Number tab, choose scientific notation and to display 3 decimal places.
The statistical parameter $R^2$ is the (often misused) correlation coefficient. A perfectly straight line will give a $R^2$ of exactly 1. Play around with the range of data you plot until your $R^2$ is very close to 1. When you are satisfied, print out and include this plot in your notebook (I chose to include my data from 13.70 to 14.50 mL):

![Final Gran Plot](image)

Use this plot to determine (yet another) value for $V_e$, solving for $V_e$ algebraically.

(6) Finally, we will use the slope of your final Gran plot (which is equal to $-\frac{\gamma_{HP}}{\gamma_{P^2-}} K_a$) to determine a value for $K_a$. 
(a) Use the LINEST function to fit the same points plotted in your final Gran plot. (The slope, y-intercept, and correlation coefficient computed by LINEST should be identical to what Add Trendline reports.)
(b) Next, compute the total ionic strength of the solution close to the endpoint. Clearly, $\mu$ is increasing throughout the titration. We will choose arbitrarily to compute $\mu$ at around the midway point of our final Gran plot: $0.95V_e$, where we use the $V_e$ determined from the Gran plot. Consider the contributions of $K^+$, $Na^+$, HP$^-$ and P$^{2-}$. (Think about why it is safe to neglect the contributions of H$^+$ and OH$^-$.)
(c) Next, determine activity coefficients (at the ionic strength determined in (b)) for HP$^-$ and P$^{2-}$, assuming that both ions have a hydrated radius $\alpha = 600$ pm. Note that you will have to interpolate the values in Harris Table 8-1 or use the extended Debye-Huckel equation.
(d) Compute $K_a$. Using the standard error in the slope computed by LINEST, also determine the standard error and the 95% confidence interval for $K_a$.
(e) By performing the appropriate $t$-test, determine if there is a significant difference between the literature value for $K_2$ of phthalic acid and your $K_a$ value. If there is, briefly comment on possible reasons for this discrepancy.